

Improving Global Tide Models Using GRACE Data

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Overview:

Estimates of tidal errors (in GOT4.7)
obtained from analysis of GRACE Level 1-B
data (R. D. Ray, B. Loomis, S. Luthcke)

→ Suitable for re-processing GRACE
range-rate data (or other POD)

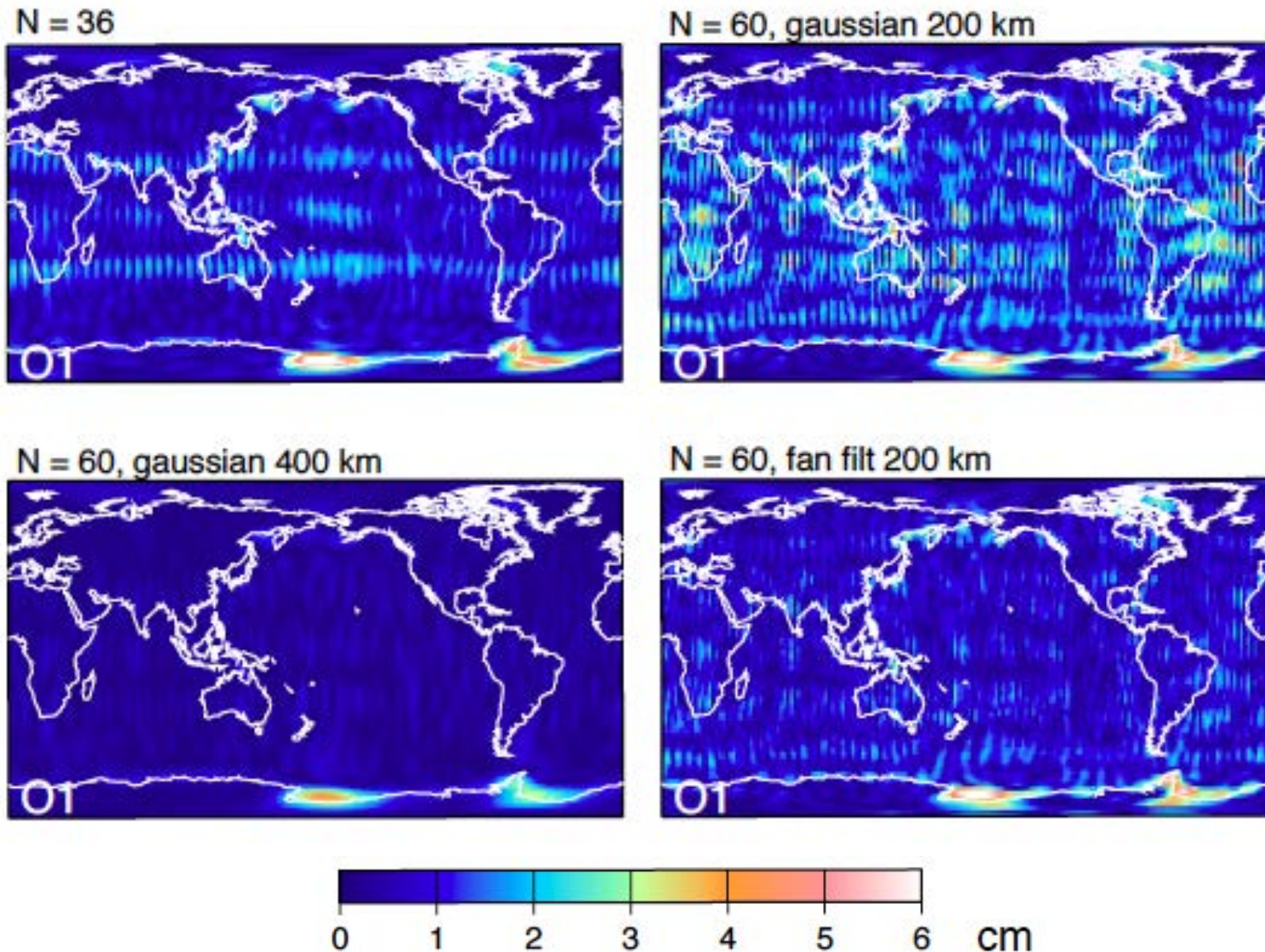
Here we discuss assimilation of the GRACE
analysis into a global hydrodynamic tide
model (TPXO.#)

→ Improve global tide models for a
broader range of applications

Tide Inversion Methodology

1. Analyze GRACE Level-1B data; need at least 7 full years (K1 alias period).
2. Tides parameterized in spherical harmonics, up to $N = 90$.
3. Initial experiments suggest constituents can be estimated one at a time.
4. Forward modeling of non-tidal variability
ECMWF operational atmosphere (includes air tides)
MOG2D barotropic ocean
GSFC GRACE land (not ocean) mascons: ice + hydrology
5. Simultaneous arc-parameter adjustments
6. Prior tide model:
short periods - GOT4.7 long periods - TPXO6.2

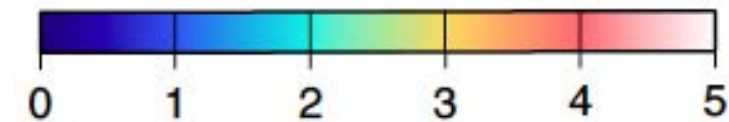
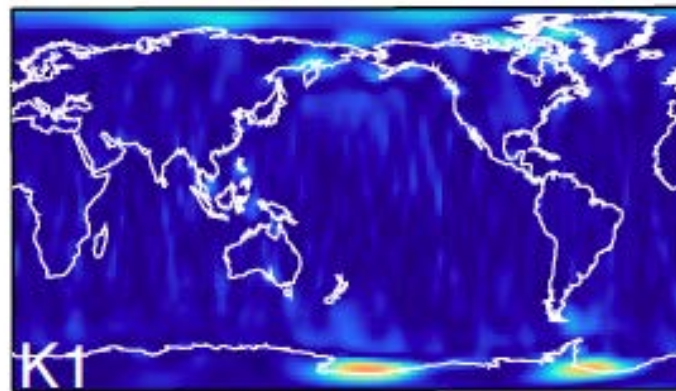
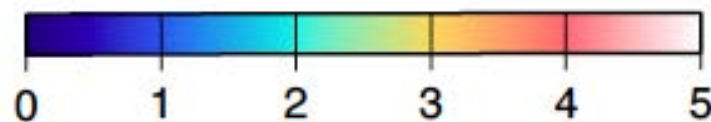
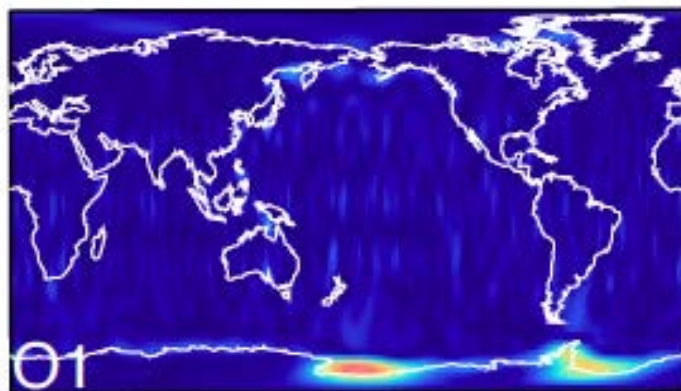
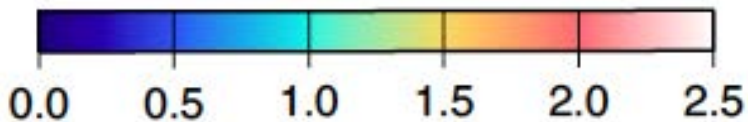
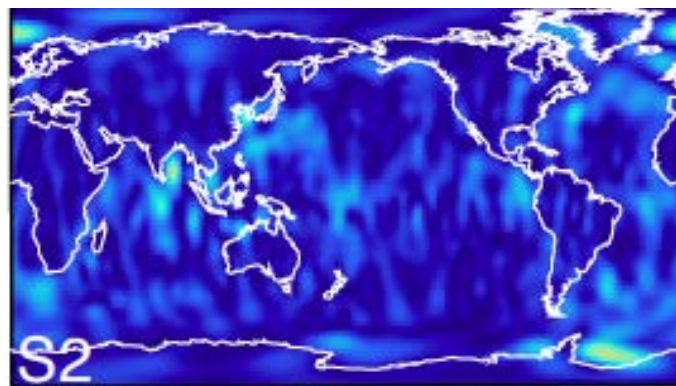
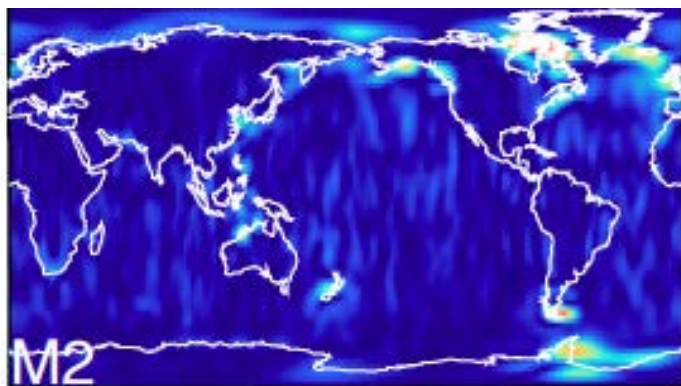
Solutions must be smoothed to be useful: Example of O1



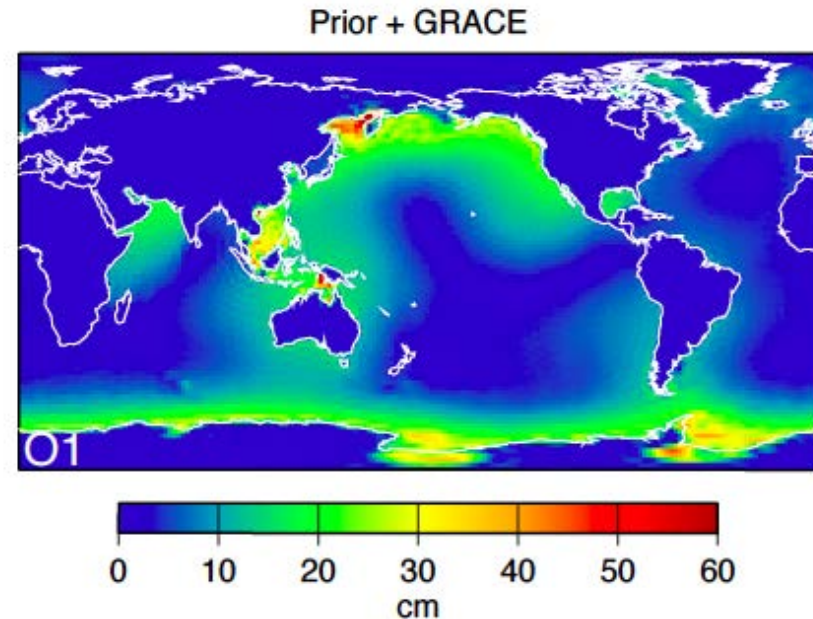
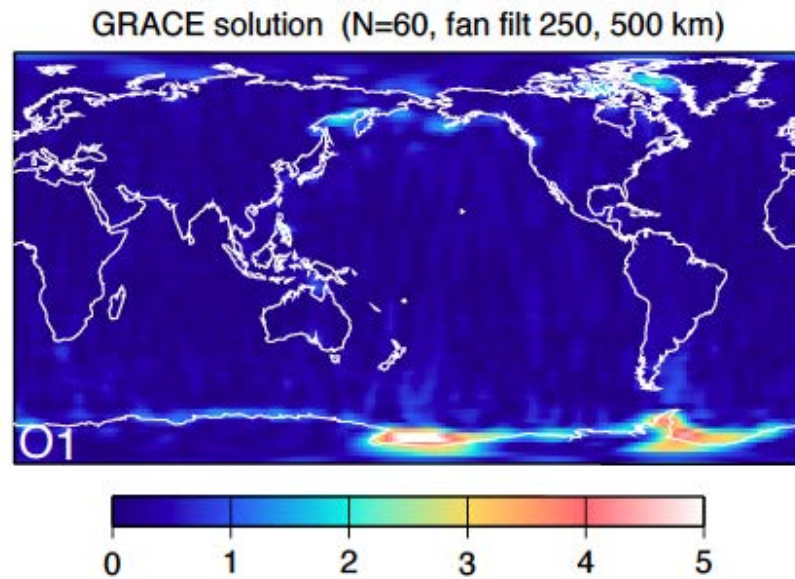
GRACE Tide Solutions

Relative to prior tide model

Gaussian smoothing $r = 400$ km Units: cm

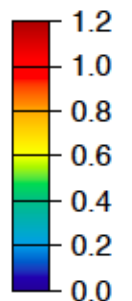
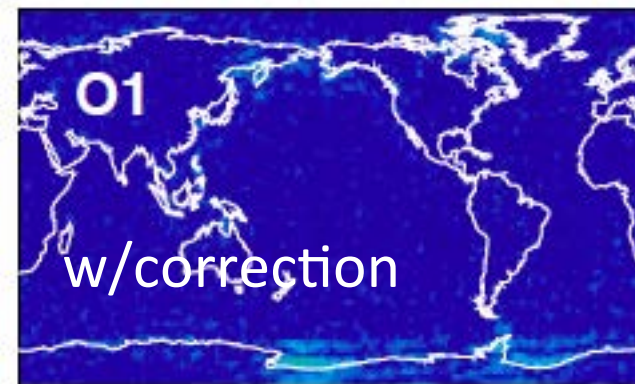
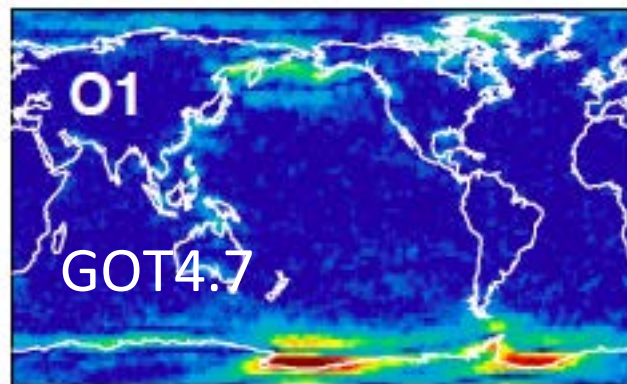


Smoothed GRACE solution + Prior Model

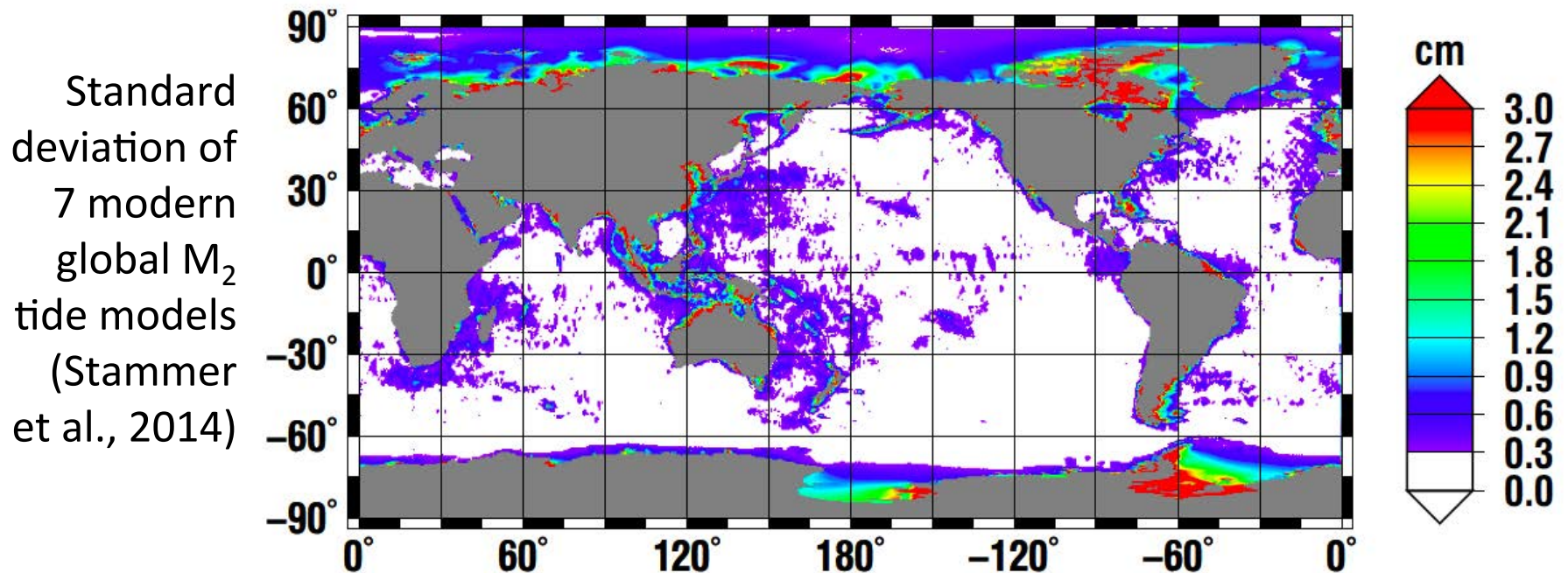


→ improved tide model for GRACE processing

GRACE
Accel.
Residuals
(nm / s²)



The GRACE tidal solutions could help improve global tide models, especially at high latitudes where errors are still large



We are working toward incorporating constraints from GRACE into a data-assimilating global tide model (TPXO.#)

Variational Data Assimilation

Estimate state (e.g., tidal height + currents) combining :

Dynamical
equations

$$\mathbf{S}\mathbf{u} = \mathbf{f} + \delta\mathbf{f}$$

Allow for errors in
dynamical equations
(forcing, boundary
conditions, missing
physics) and data

Data

$$\mathbf{d} = \mathbf{L}\mathbf{u} + \delta\mathbf{d}$$

Minimize penalty functional

$$\varphi(\mathbf{u}) = (\mathbf{d} - \mathbf{L}\mathbf{u})^* \Sigma_{\mathbf{d}}^{-1} (\mathbf{d} - \mathbf{L}\mathbf{u}) + (\mathbf{S}\mathbf{u} - \mathbf{f})^* \Sigma_{\mathbf{f}}^{-1} (\mathbf{S}\mathbf{u} - \mathbf{f})$$

Error covariances encode a priori beliefs about magnitude,
spatial/temporal correlation structure of errors in forcing,
boundary and initial conditions, data

Representer Approach: Implemented in OSU Tidal Inversion Software (OTIS)

Can show: $\hat{\mathbf{u}} = \mathbf{u}_0 + \sum_k \beta_k \mathbf{r}_k$ ← **representers:**
 obtained by solving

$\mathbf{S}^* \lambda_k = L_k$ $\mathbf{S} \mathbf{r}_k = \Sigma_f \lambda_k$

$\nearrow$
Prior model

Solve adjoint, forward problem for each observation

Coefficients $\mathbf{b}$ satisfy: $[\mathbf{R} + \Sigma_d] \mathbf{b} = \mathbf{d} - \mathbf{L}^* \mathbf{u}_0$

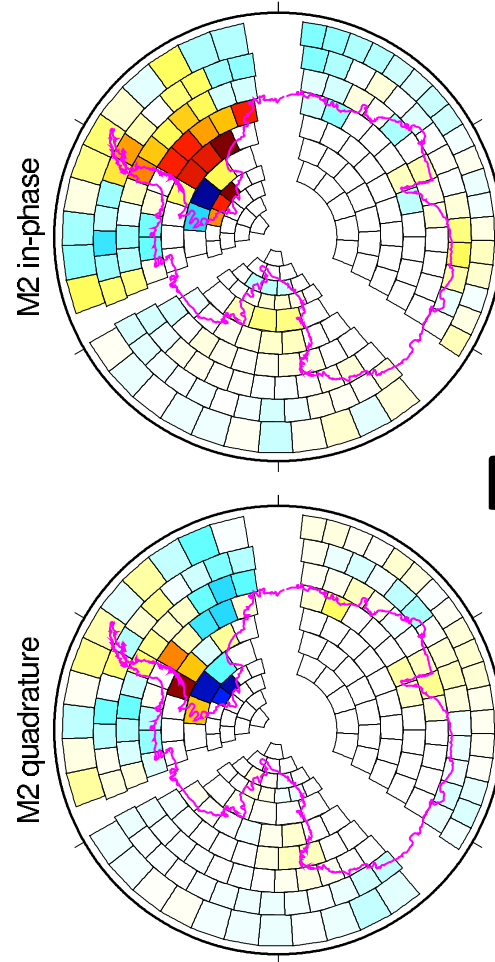
$\nearrow$
Representer matrix

$R_{jk} = L_j^* \mathbf{r}_k$

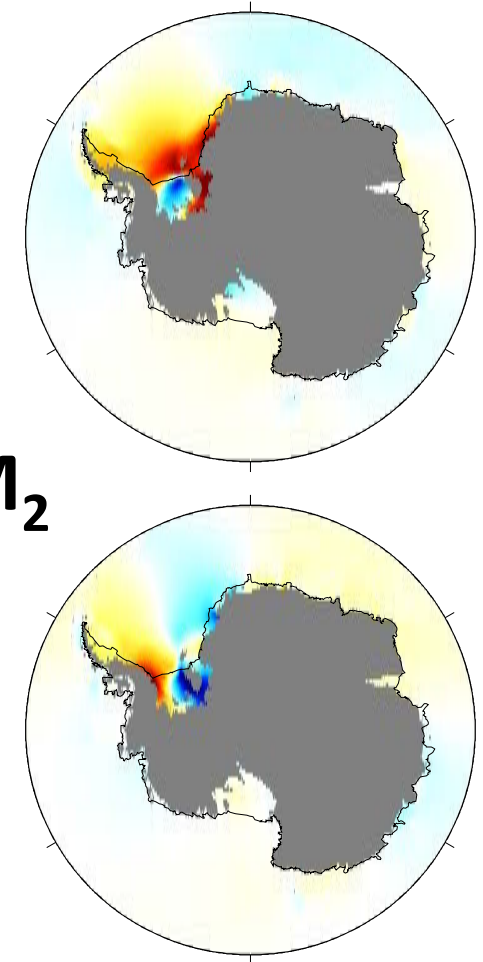
dynamically consistent basis functions

Earlier effort using OTIS:
Egbert et al., 2009
assimilation of tidal
solutions around
Antarctica from 4 years
of GRACE data
(2003-2007),
parameterized as
MASCONS

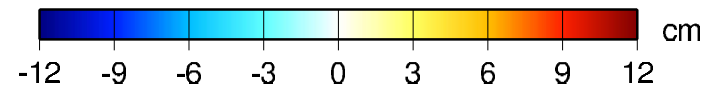
MASCONS from GRACE



Correction to TPXO.7



M_2



Representers for spherical harmonic coefficients

$$\hat{\mathbf{u}} = \mathbf{u}_0 + \sum_k \beta_k \mathbf{r}_k \leftarrow \text{representers:}$$

obtained by solving

$$\mathbf{S}^* \boldsymbol{\lambda}_k = L_k \quad \mathbf{S} \mathbf{r}_k = \Sigma_f \boldsymbol{\lambda}_k$$

↑

Prior
model

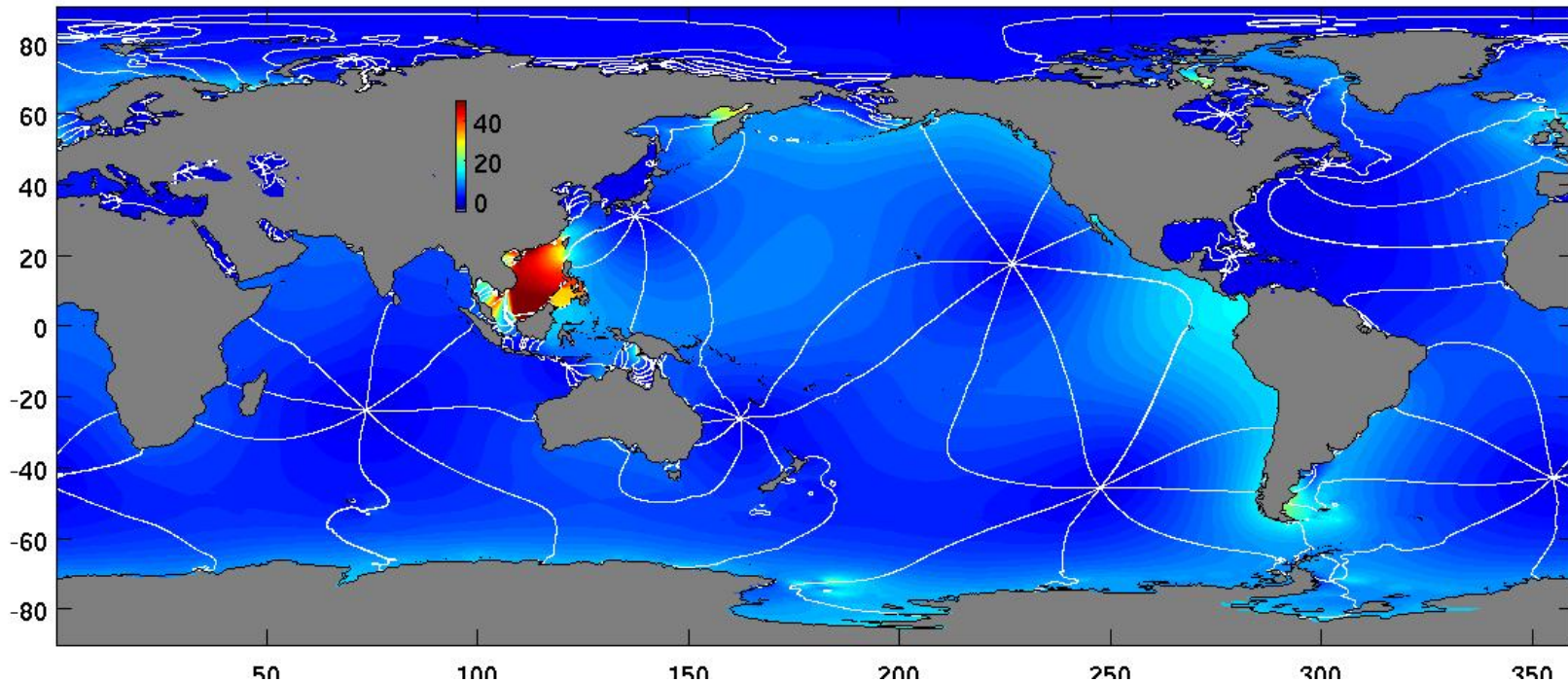
Solve adjoint equations with
spherical harmonic forcing (L_k)

Representer
matrix

$$R_{jk} = L_j^* \mathbf{r}_k$$

essentially: expand
representer in spherical
harmonics

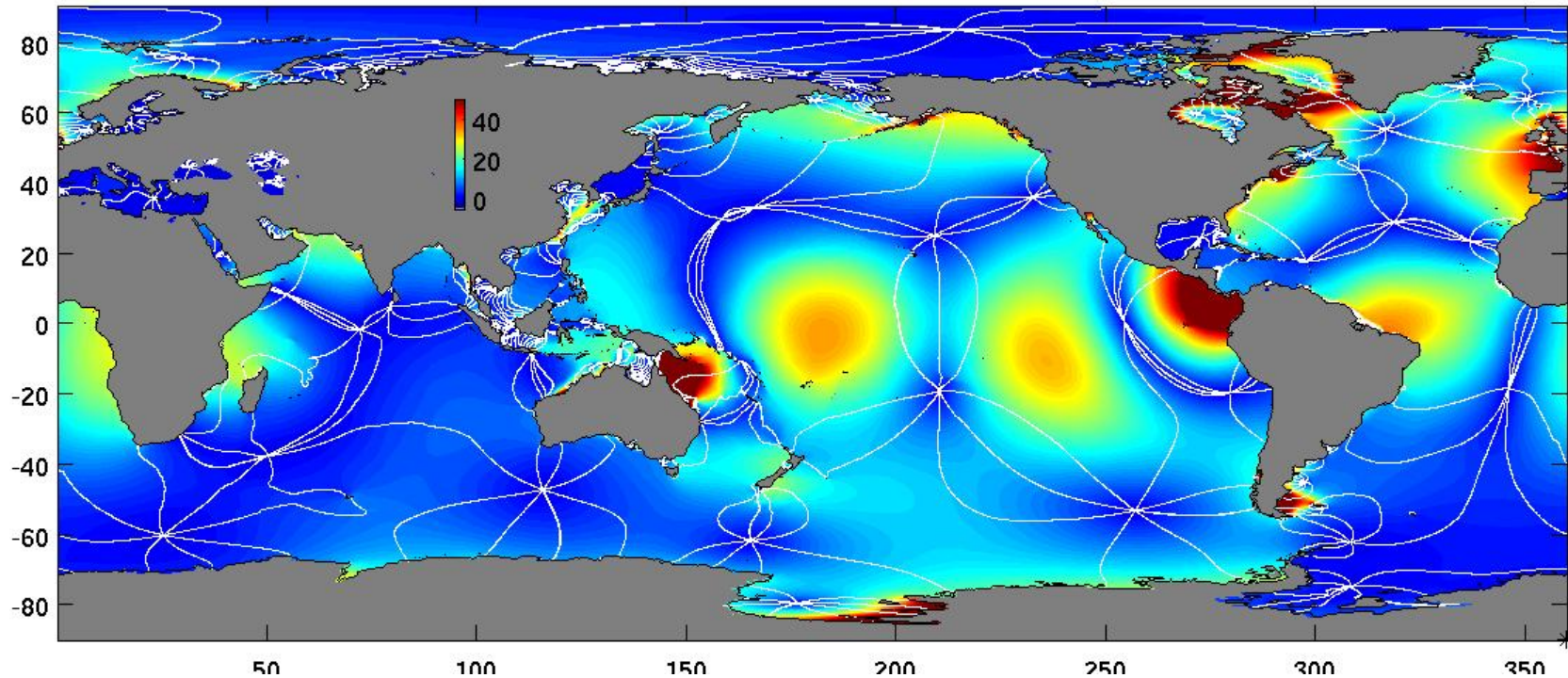
Examples of Representers: $O_1 : Y_2^{-2}$



dynamically consistent basis functions

Note that dynamics of the tides strongly influence representers!

Examples of Representers: $O_1 : Y_2^{-2}$



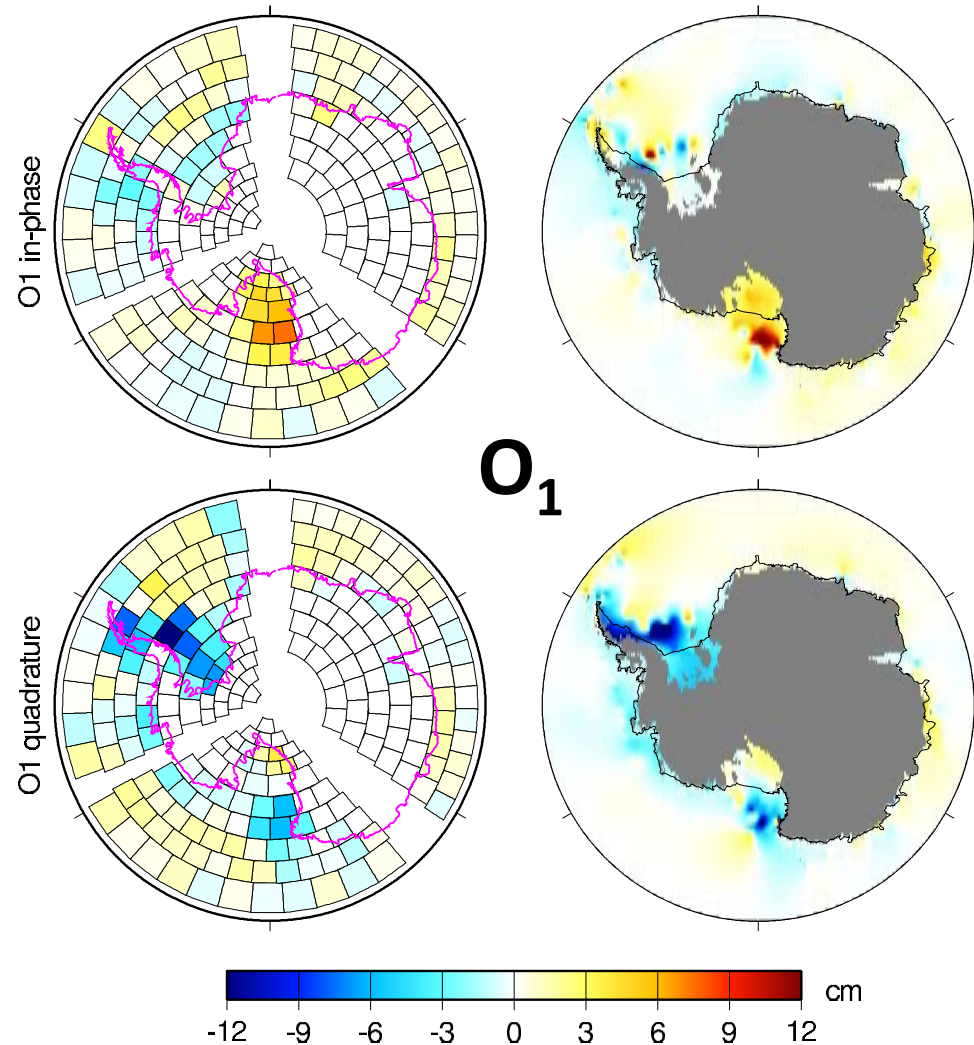
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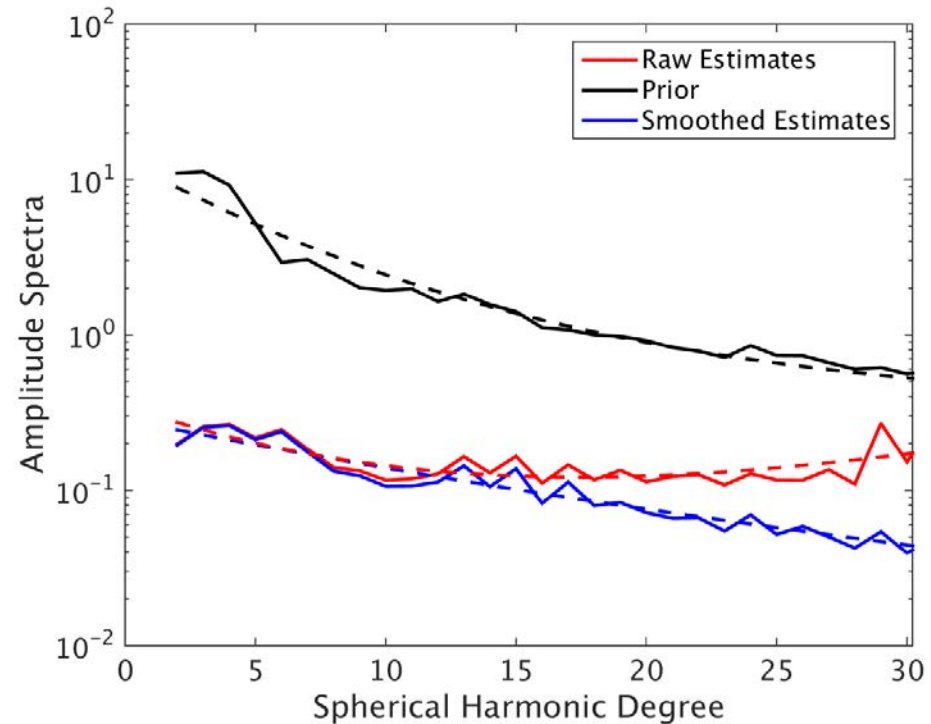
Correction to TPXO.7



Also need data error covariance (Σ_d)

**First cut:
ad hoc, based on
spectra of tidal
models, GRACE
solution**

**Plan to use full
covariance from
GRACE analysis**



Inverse solutions (still working on this!):

- Initially just invert GRACE spherical harmonics to estimate correction to existing global assimilation solution TPXO.8**
- Ultimately: simultaneous inversion of multi-satellite altimetry data and GRACE**
- Seawater density: another issue that needs attention**

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